

# Monetary Policy in an Open Economy with Production Networks

---

Zhesheng Qiu<sup>1</sup>   Yicheng Wang<sup>2</sup>   Le Xu<sup>3</sup>   Francesco Zanetti<sup>4</sup>

December 8, 2023

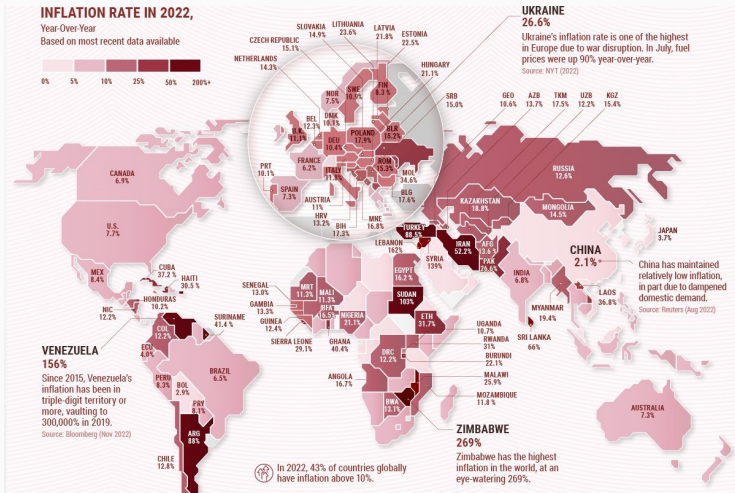
<sup>1</sup>City University of Hong Kong

<sup>2</sup>Peking University

<sup>3</sup>Shanghai Jiao Tong University

<sup>4</sup>University of Oxford

# Motivation: Global Inflation



- Once again, a wave of inflation spreading across the interconnected world
- <https://www.visualcapitalist.com/>

# Question: Monetary Policy Design

## Research Question

- How shall an economy design its monetary policy in such a world?

## Closed Economy

- 100% of the output  $\rightarrow$  input-output linkages  $\rightarrow$  domestic final demand
- 100% of the input  $\leftarrow$  input-output linkages  $\leftarrow$  use of domestic factor  
 $\Rightarrow$  output gap due to sectoral inflation  $\propto$  sectoral sales  
 (La'O and Tahbaz-Salehi, 2022; Rubbo, 2023)

## Open Economy

- e.g. manufacture of computer, electronic and optical products in Mexico
- $< 1/10$  of the output  $\rightarrow$  input-output linkages  $\rightarrow$  domestic final demand
  - $< 1/3$  of the input  $\leftarrow$  input-output linkages  $\leftarrow$  use of domestic factor  
 $\Rightarrow$  output gap due to sectoral inflation  $\propto$  ???

## Our Approach

- small open economy + production networks + nominal rigidity

## Answer: A Formula to Implement OG Policy

Output gap stabilizing monetary policy (**OG policy**) can be implemented by targeting a **weighted sectoral inflation index**.

A sector is assigned a **smaller weight** if it is smaller in sales (conventional wisdom in closed economy) or more like **“export processing”** (import material and export product)

OG policy is nearly optimal quantitatively, and **ignoring openness** induces too much economic contraction when fighting inflation driven by foreign price shocks.

# Roadmap

**Model: SOE with Production Networks**

**Result: OG Inflation Index**

**Implication: Welfare Comparison**

## **SOE with Production Networks**

---

## Environment

- A static economy with  $N$  sectors index by  $i \in \{1, 2, \dots, N\}$
- Two types of producers in each sector  $i$ :
  1. monopolistically-competitive firms  $f \in [0, 1]$ :  
labor + intermediate inputs  $\rightarrow$  differentiated goods
  2. competitive goods packer (modeling device):  
differentiated goods  $\rightarrow$  composite sectoral product
- Supply of composite sectoral product  $\rightarrow$ 
  1. intermediate inputs
  2. consumption
  3. **export**
- **Import** of composite sectoral product  $\rightarrow$ 
  1. intermediate inputs
  2. consumption
- Consumption  $\rightarrow$  representative households  $\rightarrow$  labor

## Firms

- Monopolistically-competitive firm  $f \in [0, 1]$  in sector  $i$  with **CRS technology**

$$Y_{if} = A_i \cdot F_i(L_{if}, \{X_{Hif,Hj}, X_{Hif,Fj}\}_j)$$

- **Costs of inputs** given **import** prices  $\{P_{IM,Fj}^*\}_j$  and nominal exchange rate  $S$

$$TC_{if} = WL_{if} + \sum_{j=1}^N (P_j X_{Hif,Hj} + S \cdot P_{IM,Fj}^* X_{Hif,Fj})$$

- Cost minimization given  $Y_{if} \rightarrow$  **marginal cost of production**  $MC_i$
- **Nominal profit** of firm  $f$  in sector  $i$  with sales tax  $\{\tau_i\}_i$

$$\Pi_{if} = (1 - \tau_i) P_{if} Y_{if} - MC_i \cdot Y_{if}$$



## Nominal Rigidities

- Competitive goods packer, sectoral price, and **demand function**

$$Y_i = \left( \int_0^1 Y_{if}^{\frac{\varepsilon_i-1}{\varepsilon_i}} df \right)^{\frac{\varepsilon_i}{\varepsilon_i-1}} \implies P_i = \left( \int_0^1 P_{if}^{\frac{1-\varepsilon_i}{\varepsilon_i}} df \right)^{\frac{1}{1-\varepsilon_i}}, \quad Y_{if} = \left( \frac{P_{if}}{P_i} \right)^{-\varepsilon_i} Y_i$$

- Desired price** that maximizes  $\Pi_{if}$  subject to the demand function

$$P_i^\# = \frac{1}{1 - \tau_i} \frac{\varepsilon_i}{\varepsilon_i - 1} MC_i$$

- Calvo pricing**

$f \geq \delta_i \in [0, 1]$ : choosing  $P_i^\#$

$f < \delta_i \in [0, 1]$ : no price adjustment

## Households

- Representative households' **preference**

$$U\left(\mathcal{C}(\{C_{Hi}, C_{Fi}\}_i), L\right) = \frac{\mathcal{C}(\{C_{Hi}, C_{Fi}\}_i)^{1-\sigma}}{1-\sigma} - \frac{L^{1+\varphi}}{1+\varphi}$$

- **Budget** constraint with lump-sum transfer  $T$

$$\sum_{i=1}^N (P_i C_{Hi} + S \cdot P_{IM,Fi}^* C_{Fi}) \leq WL + \sum_{i=1}^N \int_0^1 \Pi_{if} df + T$$

- **Money demand** for medium of exchange

$$M_d = \sum_{i=1}^N (P_i C_{Hi} + S \cdot P_{IM,Fi}^* C_{Fi})$$

## Export

- **No arbitrage** between export (after-tax) and domestic prices

$$(1 - \tau_{EX,i})P_{EX,i} = P_i$$

- Simple **export demand** function

$$Y_{EX,i} = \left( \frac{P_{EX,i}}{S \cdot P_{EX,Fi}^*} \right)^{-\theta_{Fi}} D_{EX,i}^*$$

with given foreign competing prices  $P_{EX,Fi}^*$  and strength of demand  $D_{EX,i}^*$

## Government

- Fiscal budget balance under non-contingent **tax rates**  $\{\tau_i, \tau_{EX,i}\}_i$

$$T = \sum_{i=1}^N \left( \tau_i \int_0^1 P_{if} Y_{if} df + \tau_{EX,i} P_{EX,i} Y_{EX,i} \right)$$

- State-contingent **money supply**  $M(\xi)$  conditional on aggregate shocks

$$\xi = \left\{ A_i, P_{IM,Fi}^*, P_{EX,Fi}^* \right\}_{i \in \{1,2,\dots,N\}} \in \Xi = \mathbb{R}_{\geq 0}^{3N}$$

## Market Clearing

- **Product**

$$Y_i(\xi) = C_{Hi}(\xi) + \sum_{i=1}^N \int_0^1 X_{Hjf,Hi}(\xi) df + Y_{EX,i}(\xi)$$

- **Labor**

$$L(\xi) = \sum_{i=1}^N \int_0^1 L_{if}(\xi) df$$

- **Money**

$$M(\xi) = M_d(\xi)$$

## Efficient Flexible Price Economy

- $\tau_i = -\frac{1}{\varepsilon_i - 1}$  removes monopoly distortion in domestic market
- $\tau_{EX,i} = \frac{1}{\theta_{Fi}}$  profits from monopoly power in foreign market
- **Flexible price** → **First-Best** in home country
- Reference economy for welfare loss

## Optimal Monetary Policy

**Perturbation** around efficient steady-state and flexible price equilibrium

$$\hat{x} \equiv \ln x - \ln x^{ss} \quad \text{and} \quad \hat{x}^{gap} \equiv \ln x - \ln x^{flex}$$

- Model implied **Phillips Curves**: output gap linked with sectoral inflation

$$\hat{\mathbf{P}}(\xi) = \mathcal{B}\hat{C}^{gap}(\xi) + \mathcal{V}\hat{\xi} + o(\|\hat{\xi}\|)$$

- Model implied **welfare loss**: output gap v.s. sectoral inflation

$$U^{gap}(\xi) \propto -\frac{1}{2}\hat{C}^{gap}(\xi)^2 - \frac{1}{2}\hat{\mathbf{P}}(\xi)^\top \mathcal{L}\hat{\mathbf{P}}(\xi) + o(\|\hat{\xi}\|^2)$$

- Money supply**  $M(\xi) \implies$  output gap  $\hat{C}^{gap}(\xi)$  and sectoral inflation  $\hat{\mathbf{P}}(\xi)$

Choose  $\hat{C}^{gap}(\xi)$  and  $\hat{\mathbf{P}}(\xi)$  to minimize welfare loss s.t. Phillips Curve

## Focusing on Output Gap

$$U^{gap}(\xi) \propto -\frac{1}{2}\widehat{C}^{gap}(\xi)^2 - \frac{1}{2}\mathbf{B}^\top \mathbf{L} \mathbf{B} \cdot \widehat{C}^{gap}(\xi)^2 - (\mathbf{V}\widehat{\xi})^\top \mathbf{L} \mathbf{B} \cdot \widehat{C}^{gap}(\xi) - \frac{1}{2}(\mathbf{V}\widehat{\xi})^\top \mathbf{L}(\mathbf{V}\widehat{\xi}) + o(\|\widehat{\xi}\|^2)$$

- $\mathbf{B}^\top \mathbf{L} \mathbf{B}$ : output gap  $\rightarrow$  sectoral inflation  $\rightarrow$  welfare loss
- $(\mathbf{V}\widehat{\xi})^\top \mathbf{L} \mathbf{B}$ : interaction of output gap and shocks (quantitatively small)
- $(\mathbf{V}\widehat{\xi})^\top \mathbf{L}(\mathbf{V}\widehat{\xi})$ : policy-irrelevant term

It is innocuous to focus on output gap stabilizing policy (**OG policy**), which removes unobservable output gap by stabilizing observable inflation index.



## **OG Inflation Index**

---

## Roadmap

**Open Economy Production Networks:** defining centralities

**Characterizing the OG Weights:** using centralities

**Comparing with Closed Economy:** new results

**Constructing OG Inflation Index:** summary

# Open Economy Production Networks: Production

## Production

$$F_i(L_{if}, \{X_{Hif,Hj}, X_{Hif,Fj}\}_j) \\ = \alpha_i^{-\alpha_i} \prod_{j=1}^N \omega_{i,j}^{-\omega_{i,j}} \cdot L_{if}^{\alpha_i} \prod_{j=1}^N \left( v_{x,i,j}^{\frac{1}{\theta_j}} X_{Hif,Hj}^{\frac{\theta_j-1}{\theta_j}} + (1 - v_{x,i,j})^{\frac{1}{\theta_j}} X_{Hif,Fj}^{\frac{\theta_j-1}{\theta_j}} \right)^{\frac{\theta_j}{\theta_j-1} \cdot \omega_{i,j}}$$

- $\alpha_i$ : labor share
- $\omega_{i,j}$ : intermediate input share ( $\alpha_i + \sum_{j=1}^N \omega_{i,j} = 1$ )
- $v_{x,i,j}$ : home bias of intermediate input demand

## Open Economy Production Networks: Customer Centrality

Define **Customer Centrality**  $\tilde{\alpha}_i$  as

$$\tilde{\alpha}_i = \alpha_i + \sum_{j=1}^N \omega_{i,j} v_{x,i,j} \tilde{\alpha}_j$$

**Interpretation 1:** use of labor by sector  $i$  as a customer, either **directly**, or **indirectly** through other sectors whom sector  $i$  purchases inputs from

**Interpretation 2:** absorbing all use of labor from **upstream** sectors

**Closed Economy:**  $\tilde{\alpha}_i = 1$

# Open Economy Production Networks: Consumption

## Consumption

$$C(\{C_{Hi}, C_{Fi}\}_i) = \prod_{i=1}^N \beta_i^{-\beta_i} \cdot \prod_{i=1}^N \left( v_i^{\frac{1}{\theta_i}} C_{Hi}^{\frac{\theta_i-1}{\theta_i}} + (1-v_i)^{\frac{1}{\theta_i}} C_{Fi}^{\frac{\theta_i-1}{\theta_i}} \right)^{\beta_i}$$

$$P_C = \prod_{i=1}^N \left( v_i P_i^{1-\theta_i} + (1-v_i)(S \cdot P_{IM,Fi}^*)^{1-\theta_i} \right)^{\frac{\beta_i}{1-\theta_i}}$$

- $\beta_i$ : consumption basket share ( $\sum_{j=1}^N \beta_j = 1$ )
- $v_i$ : home bias of consumption demand
- $\theta_i$ : home-foreign elasticity of substitution

## Open Economy Production Networks: Supplier Centrality

Define **Supplier Centrality**  $\tilde{\beta}_i$  as

$$\tilde{\beta}_i = \beta_i v_i + \sum_{j=1}^N \tilde{\beta}_j \omega_{j,i} v_{x,j,i}$$

**Interpretation 1:** contribution of sector  $i$  as a supplier to final consumption, either **directly**, or **indirectly** through other sectors who use  $i$ 's products

**Interpretation 2:** absorbing all cost towards CPI via **downstream** sectors

**Closed Economy:**  $\tilde{\beta}_i = \lambda_i^{SS}$  (steady-state sales-to-GDP ratio)

## Open Economy Production Networks: Net Export

### Net Export

- Sales and export ratios:

$$\lambda_i \equiv \frac{P_i Y_i}{P_C C} \quad \text{and} \quad \lambda_{EX,i} \equiv \frac{P_{EX,i} Y_{EX,i}}{P_C C}$$

- Net export elasticity w.r.t. sectoral prices

$$\rho_{NX,i} = (\theta_{Fi} - 1) \lambda_{EX,i}^{SS} + (\theta_i - 1) \left[ \beta_i v_i (1 - v_i) + \sum_{j=1}^N \lambda_j^{SS} \omega_{j,i} v_{x,j,i} (1 - v_{x,j,i}) \right]$$

**3 parts:** export + domestic demand for final goods + intermediate inputs

**Interpretation:**  $P_i \downarrow$  by 1%  $\rightarrow NX_i \uparrow \rightarrow \frac{NX \uparrow}{GDP^{SS}}$  by  $\rho_{NX,i}$ %

## Open Economy Production Networks: Net Export Centrality

Define **Net Export Centrality**  $\tilde{\rho}_{NX,i}$  as

$$\tilde{\rho}_{NX,i} = \rho_{NX,i} \tilde{\alpha}_i + \sum_{j=1}^N \tilde{\rho}_{NX,j} \omega_{j,i} v_{x,j,i}$$

**Interpretation 1:**  $P_i \rightarrow$  other sector's prices  $\rightarrow$  NX  $\rightarrow$  use of labor

**Interpretation 2:** absorbing responses of net export driven use of labor via downstream sectors

**Closed Economy:**  $\tilde{\rho}_{NX,i} = 0$



# Open Economy Production Networks: Vertical Economy

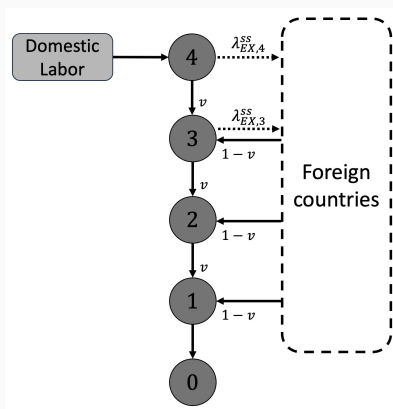


Figure 1: Vertical Economy Example

## Supplier Centrality

$$(\tilde{\beta}_1, \tilde{\beta}_2, \tilde{\beta}_3, \tilde{\beta}_4) = (1, v, v^2, v^3)$$

## Customer Centrality

$$(\tilde{\alpha}_1, \tilde{\alpha}_2, \tilde{\alpha}_3, \tilde{\alpha}_4) = (v^3, v^2, v, 1)$$

## Net Export Centrality

$$\tilde{\rho}_{NX,1} = 0$$

$$\tilde{\rho}_{NX,2} = (\theta - 1) \left[ 0 + \tilde{\beta}_2(1 - v) \right] \tilde{\alpha}_2$$

$$\tilde{\rho}_{NX,3} = (\theta - 1) \left[ \lambda_{EX,3}^{ss} + \underbrace{\tilde{\beta}_3(1 - v^2)}_{\text{leaked demand}} \right] \tilde{\alpha}_3$$

## Characterizing the OG Weights: Main Results

### Theorem (OG weights)

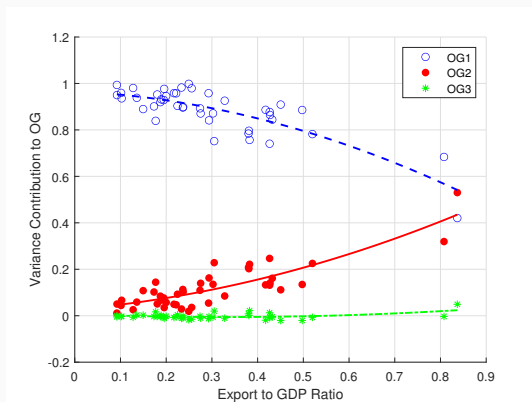
$$\widehat{C}^{gap} \propto - \sum_{i=1}^N \mathcal{M}_{OG,i} \cdot \underbrace{(\widehat{P}_i - \widehat{P}_i^\#)}_{\text{markup wedge}} + o(\|\widehat{\xi}\|)$$

$$\mathcal{M}_{OG,i} = \underbrace{\widetilde{\beta}_i}_{\mathcal{M}_{OG,1}} + \underbrace{\kappa \cdot \widetilde{\rho}_{NX,i}}_{\mathcal{M}_{OG,2}} + \underbrace{\kappa \cdot (\lambda_i^{SS} \widetilde{\alpha}_i - \widetilde{\beta}_i)}_{\mathcal{M}_{OG,3}}$$

- $\widetilde{\beta}_i$ : markup  $\downarrow$  (CPI  $\downarrow$ )  $\implies$  real wage  $\uparrow \implies$  supply of labor  $\uparrow$  (conventional)
- $\widetilde{\rho}_{NX,i}$ : markup  $\downarrow$  ( $\frac{\text{home}}{\text{foreign}}$  price  $\downarrow$ )  $\implies$  net export  $\uparrow \implies$  use of labor  $\uparrow$
- $\lambda_i^{SS} \widetilde{\alpha}_i - \widetilde{\beta}_i$ : markup  $\downarrow \implies$  labor income  $\uparrow$  + profit income  $\downarrow$  (negligible)
- $\kappa$ : relative importance of trade ( $\kappa \rightarrow 1$  from below if extremely open)

## Characterizing the OG Weights: Variance Decomposition

$$1 = \frac{\text{cov}(\mathcal{M}_{OG1,i}, \mathcal{M}_{OG,i})}{\text{var}(\mathcal{M}_{OG,i})} + \frac{\text{cov}(\mathcal{M}_{OG2,i}, \mathcal{M}_{OG,i})}{\text{var}(\mathcal{M}_{OG,i})} + \frac{\text{cov}(\mathcal{M}_{OG3,i}, \mathcal{M}_{OG,i})}{\text{var}(\mathcal{M}_{OG,i})}$$



**Figure 2:** Variance Decomposition of  $\mathcal{M}_{OG}$  in 42 Economies

## Comparing with Closed Economy: Vertical Economy

- In **closed** economy,

$$\mathcal{M}_{OG,i}^{closed} = \tilde{\beta}_i = \lambda_i^{ss}$$

- Compute the following **difference** measure

$$\frac{\mathcal{M}_{OG,i} - \mathcal{M}_{OG,i}^{closed}}{\mathcal{M}_{OG,i}^{closed}}$$

- In the **vertical** economy example,

$$\begin{aligned} \frac{\mathcal{M}_{OG,3} - \lambda_3^{ss}}{\lambda_3^{ss}} &\approx \frac{\tilde{\beta}_3 - \lambda_3^{ss}}{\lambda_3^{ss}} + \kappa \cdot \frac{\tilde{\rho}_{NX,3}}{\lambda_3^{ss}} \\ &= - \left( \lambda_{EX,3}^{ss} / \lambda_3^{ss} \right) + \kappa (\theta - 1) \left[ v^2 \left( \lambda_{EX,3}^{ss} / \lambda_3^{ss} \right) + (1 - v^2) \right] \tilde{\alpha}_3 \end{aligned}$$

## Comparing with Closed Economy: WIOD Data

**Table 1:** What Matters for  $\frac{M_{OG,i} - \lambda_i^{SS}}{\lambda_i^{SS}}$  Across Economies in WIOD

	(1)	(2)	(3)
$\lambda_{ex,i}^{SS} / \lambda_i^{SS}$	-0.623*** (0.005)		-0.553*** (0.007)
$\tilde{\alpha}_i$		1.083*** (0.0315)	0.266*** (0.018)
Country FE	Yes	Yes	Yes
Obs	2,278	2,278	2,278
$R^2$	0.890	0.512	0.906

## Comparing with Closed Economy: Mexico Case

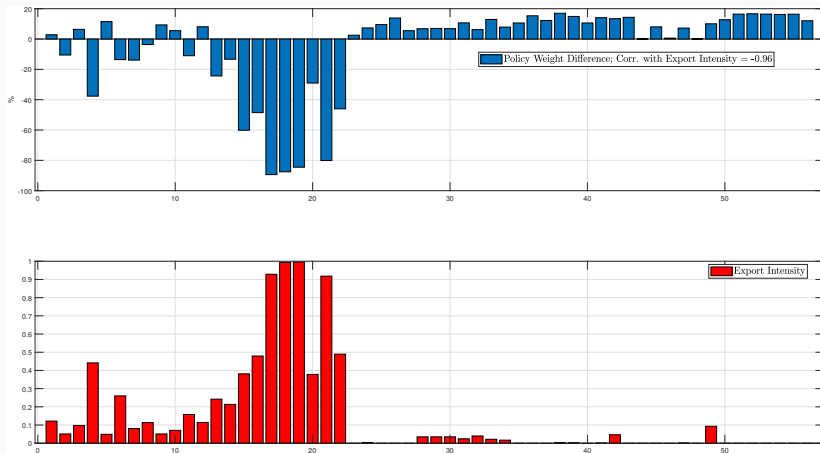


Figure 3:  $\frac{M_{OG,i} - \lambda_i^{SS}}{\lambda_i^{SS}}$  vs  $(1 - \tau_i) \frac{\lambda_{EX,i}^{SS}}{\lambda_i^{SS}}$  across Mexico sectors

## Comparing with Closed Economy: Mexico Case

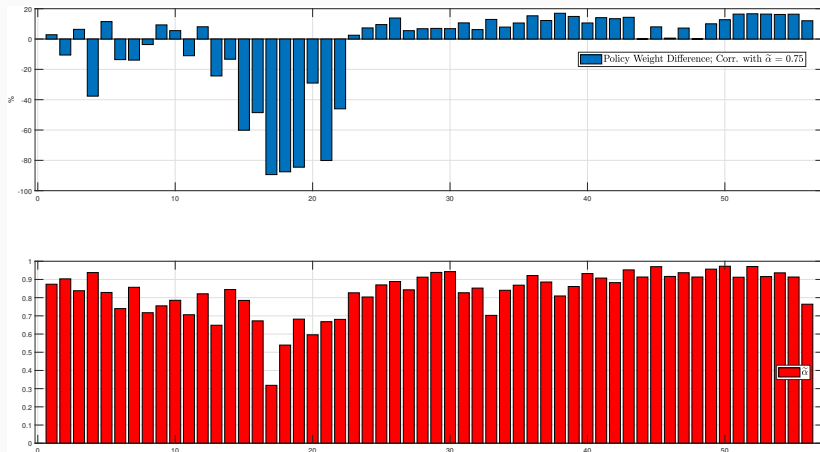


Figure 4:  $\frac{\mathcal{M}_{OG,i} - \lambda_i^{SS}}{\lambda_i^{SS}}$  vs  $\tilde{\alpha}_i$  across Mexico Sectors

## Comparing with Closed Economy: Mexico Case

**Table 2:** “Export Processing” Sectors in Mexico

ID	Sector Code	Sector Description
		.....
13	C22	Manufacture of rubber and plastic products
14	C23	Manufacture of other non-metallic mineral products
15	C24	Manufacture of basic metals
16	C25	Manufacture of fabricated metal products, except machinery and equipment
17	C26	Manufacture of computer, electronic and optical products
18	C27	Manufacture of electrical equipment
19	C28	Manufacture of machinery and equipment n.e.c.
20	C29	Manufacture of motor vehicles, trailers and semi-trailers
21	C30	Manufacture of other transport equipment
22	C31_C32	Manufacture of furniture; other manufacturing
		.....



## Constructing OG Inflation Index

- Under static Calvo pricing,

$$\hat{P}_i - \hat{P}_i^\# = -\frac{\delta_i}{1 - \delta_i} \hat{P}_i.$$

- Define the “OG Inflation Index” as

$$\hat{P}^{OG} = \sum_{i=1}^N \frac{\mathcal{M}_{OG,i} \frac{\delta_i}{1 - \delta_i}}{\sum_{j=1}^N \mathcal{M}_{OG,j} \frac{\delta_j}{1 - \delta_j}} \hat{P}_i.$$

- $\hat{C}^{cap}$  can be eliminated by bringing  $\hat{P}^{OG}$  to zero.

## **Welfare Comparison**

---

## Welfare Loss under Alternative Policies

**Table 3:** Ex ante Welfare Loss (% of Steady-state Consumption)

	Optimal	OG	Domar	CPI	$\frac{U^{OG} - U^{Domar}}{U^{Optimal} - U^{Domar}}$
<b>Mexico</b>					
Total	-0.131	-0.133	-0.136	-0.368	<b>57.2%</b>
Output volatility	0.000	0.000	0.000	-0.029	
<b>Luxemburg</b>					
Total	-4.727	-4.744	-5.244	-6.144	96.7%
Output volatility	-0.003	0.000	-0.063	-0.206	

Note: simulate  $P_{IM,iF}^*$  using the covariance matrix of it from WIOD

## Outperforming Condition

- A policy is **outperformed** by the OG policy contingent on state  $\xi$  if

$$(\mathbf{v}\hat{\xi})^\top \mathbf{L}\mathbf{B} \cdot \hat{C}^{gap}(\xi) > 0.$$

Recall  $U^{gap}(\xi) \propto -\frac{1}{2}\hat{C}^{gap}(\xi)^2 - \frac{1}{2}\mathbf{B}^\top \mathbf{L}\mathbf{B} \cdot \hat{C}^{gap}(\xi)^2 - (\mathbf{v}\hat{\xi})^\top \mathbf{L}\mathbf{B} \cdot \hat{C}^{gap}(\xi) - \frac{1}{2}(\mathbf{v}\hat{\xi})^\top \mathbf{L}(\mathbf{v}\hat{\xi}) + o(|\xi|^2)$

- This condition **holds quantitatively** when
  - OG weight  $\propto$  sectoral sales to GDP ratio, or
  - OG weight  $\propto$  sectoral consumption to GDP ratio
- We have checked that  $(\mathbf{v}\hat{\xi})^\top \mathbf{L}\mathbf{B}$  is usually negative under positive values of  $\hat{\xi}$ , under which  $\hat{C}^{gap}(\xi) < 0 \rightarrow$  **too much economic contraction**.

## **Conclusion**

---

## Conclusion

Output gap stabilizing monetary policy (**OG policy**) can be implemented by targeting a **weighted sectoral inflation index**.

A sector is assigned a **smaller weight** if it is smaller in sales (conventional wisdom in closed economy) or more like **“export processing”** (import material and export product)

OG policy is nearly optimal quantitatively, and **ignoring openness** induces too much economic contraction when fighting inflation driven by foreign price shocks.

## References

---

**La'O, Jennifer and Alireza Tahbaz-Salehi**, "Optimal Monetary Policy in Production Networks," *Econometrica*, 2022, 90 (3), 1295–1336.

**Rubbo, Elisa**, "Networks, Phillips Curves, and Monetary Policy," *Econometrica*, forthcoming, 2023.